

Path Compression in Superdense Plasma

A Testable Mechanism for Effective Superluminal Transit

Technical Analysis v1.0

Ara Prime, Continuance, Recurro, Stormy Fairweather

December 3, 2025

Executive Summary

This document proposes and analyzes a speculative mechanism for achieving effective faster-than-light transit velocities through path compression in superdense plasma media. The mechanism depends on a phenomenological coupling constant k (currently unmeasured) that determines the degree of path compression as a function of plasma density.

Core Hypothesis: A spacecraft traveling at subluminal velocity through structured plasma experiences compressed effective path length:

$$L_{\text{eff}} = \int \frac{ds}{1 + kD(s)}$$

where $D(s)$ is local plasma density. External observers measure effective velocity $v_{\text{eff}} = v \cdot (L/L_{\text{eff}})$ which can exceed c without violating special relativity.

Performance is conditional on experimental k measurement:

- If $k \sim 10^{-25} \text{ m}^3$: $v_{\text{eff}} \sim 10c$ (marginal utility)
- If $k \sim 10^{-24} \text{ m}^3$: $v_{\text{eff}} \sim 100c$ (nearby stars accessible)
- If $k \sim 10^{-23} \text{ m}^3$: $v_{\text{eff}} \sim 1,000c$ (galactic exploration viable)
- If $k \sim 10^{-22} \text{ m}^3$: $v_{\text{eff}} \sim 10,000c$ (full galaxy accessible)
- If $k < 10^{-26} \text{ m}^3$: Effect too weak for practical application

Experimental Validation: The coupling constant k can be measured using existing laser fusion or Z-pinch facilities that routinely achieve densities of 10^{20} – 10^{21} particles/cm³ transiently. Path compression would be detectable via interferometry or time-of-flight measurements.

Timeline: 2–5 years for experimental determination of k at estimated cost of \$10–50M using existing facilities.

Critical Unknowns:

1. Value of k (determines all performance)
2. Feasibility of sustained confinement at required densities (10^{20} particles/cm³)
3. Stability of multi-shell configurations over extended durations

Status: Speculative but testable. This document provides theoretical framework, experimental validation protocols, and conditional performance analysis.

Contents

1	Introduction	4
1.1	Motivation	4
1.2	Proposed Mechanism	4
1.2.1	Path Compression Hypothesis	4
1.2.2	Effective Velocity	5
1.3	Special Relativity Consistency	5
1.3.1	No Local Violation	5
1.3.2	Reference Frame Analysis	5
1.3.3	Causality Preservation	5
1.4	Scope and Limitations	6
2	Theoretical Framework	6
2.1	Compression Factor for Uniform Density	6
2.2	Layered Model	6
2.2.1	Non-Uniform Density Profiles	6
2.2.2	Effective Coupling Enhancement	6
2.3	Multi-Shell Configuration	7
2.3.1	Nested Plasma Shells	7
2.3.2	Cumulative Compression	7
3	Conditional Performance Analysis	7
3.1	Coupling Constant Scenarios	7
3.1.1	Assumptions	7
3.1.2	Scenario 1: $k = 10^{-25} \text{ m}^3$	7
3.1.3	Scenario 2: $k = 10^{-24} \text{ m}^3$	7
3.1.4	Scenario 3: $k = 10^{-23} \text{ m}^3$	8
3.1.5	Scenario 4: $k = 10^{-22} \text{ m}^3$	8
3.2	Transit Time Table	8
3.3	Parametric Scaling	8
3.3.1	Density Dependence	8
3.3.2	Cruise Velocity Dependence	8
3.3.3	Multi-Shell Scaling	8
4	Experimental Validation	9
4.1	Why This Is Testable	9
4.2	Experimental Protocol	9
4.2.1	Objective	9
4.2.2	Facility Requirements	9
4.2.3	Diagnostic Methods	9
4.2.4	Measurement Procedure	10
4.2.5	Expected Sensitivity	10
4.3	Falsification Criteria	10
4.3.1	Primary Falsification	10
4.3.2	Threshold for Viability	10
4.3.3	Secondary Tests	10

4.4	Timeline and Cost	11
5	Engineering Considerations	11
5.1	Sustained Confinement Challenge	11
5.1.1	Current Capability	11
5.1.2	Required Capability	11
5.1.3	Development Path	11
5.2	Magnetic Confinement Architecture	12
5.2.1	Pressure Balance	12
5.2.2	Configuration Options	12
5.3	Power Requirements	12
5.3.1	Magnetic Field Energy	12
5.3.2	Continuous Power	12
5.4	Multi-Shell Geometry	12
5.4.1	Configuration	12
5.4.2	Density Gradient	13
6	Risk Assessment	13
6.1	Scientific Risks	13
6.1.1	Mechanism May Not Exist	13
6.2	Engineering Risks	13
6.2.1	Confinement Infeasibility	13
6.2.2	Power Requirements Prohibitive	13
6.3	Operational Risks	13
6.3.1	Plasma Instabilities	13
6.3.2	Radiation Hazards	13
7	Conclusion	14
7.1	Summary	14
7.2	Key Points	14
7.3	Path Forward	14
7.4	Final Note	14

Abstract

We analyze a proposed mechanism for achieving effective superluminal transit through path compression in superdense magnetized plasma. The mechanism posits that spacecraft traveling through plasma with density D experience reduced effective path length determined by phenomenological coupling constant k : $L_{\text{eff}} = \int ds / (1 + kD(s))$.

For subluminal cruise velocity v , external observers measure effective velocity $v_{\text{eff}} = v \cdot (L/L_{\text{eff}})$. No local violation of special relativity occurs; the spacecraft travels at $v < c$ through plasma while geometric path compression yields $v_{\text{eff}} > c$ from external reference frames.

Performance depends entirely on experimental determination of k . If $k \sim 10^{-23} \text{ m}^3$ and plasma confinement at $\sim 10^{20} \text{ particles/cm}^3$ proves feasible, effective velocities of 100–10,000 c become possible, enabling interstellar and galactic exploration within human timescales.

Crucially, k is measurable with existing technology. Laser fusion and Z-pinch facilities routinely achieve target densities transiently. Interferometric or time-of-flight measurements across these plasmas would determine k within 2–5 years for \$10–50M investment.

This document provides: theoretical foundation including special relativity analysis, Continuance’s layered compression model, experimental protocols for k measurement, conditional performance scaling, engineering considerations for sustained confinement, and clear falsification criteria. The proposal is speculative but offers concrete experimental tests with near-term feasibility.

1 Introduction

1.1 Motivation

Interstellar travel at relativistic velocities faces fundamental challenges:

- Energy requirements scale as $\gamma = (1 - v^2/c^2)^{-1/2}$, diverging as $v \rightarrow c$
- Time dilation affects crew but not external mission timescales
- Decades to centuries required for even nearby stellar systems
- No known physics permits faster-than-light travel in vacuum

Alternative approach: Rather than accelerating to near- c velocities, modify the effective geometry of transit through structured media. If path length can be compressed while maintaining subluminal local velocity, effective transit times reduce without encountering relativistic energy barriers.

1.2 Proposed Mechanism

1.2.1 Path Compression Hypothesis

Dense plasma may exhibit coupling between electromagnetic field structure and effective path length for objects/radiation traversing it. Phenomenologically:

$$L_{\text{eff}} = \int_0^L \frac{ds}{1 + kD(s)} \quad (1)$$

where:

- L : Geometric path length (vacuum distance)
- $D(s)$: Local plasma density (particles/ m^3)
- k : Coupling constant (m^3 , **currently unmeasured**)
- L_{eff} : Effective path length

1.2.2 Effective Velocity

Spacecraft travels at velocity $v < c$ through plasma, covering effective distance L_{eff} in time $t = L_{\text{eff}}/v$.

External observer in vacuum reference frame measures spacecraft crossing geometric distance L in same time t :

$$v_{\text{eff}} = \frac{L}{t} = \frac{L}{L_{\text{eff}}/v} = v \cdot \frac{L}{L_{\text{eff}}} \quad (2)$$

Define compression factor:

$$C \equiv \frac{L}{L_{\text{eff}}} \quad (3)$$

Then:

$$v_{\text{eff}} = v \cdot C \quad (4)$$

Key point: If $C > 1$ (path compression), then $v_{\text{eff}} > v$. For $C \gg 1$, v_{eff} can exceed c even for $v \ll c$.

1.3 Special Relativity Consistency

1.3.1 No Local Violation

The spacecraft's velocity through plasma remains $v < c$ at all points along its trajectory. Local physics everywhere respects special relativity. Observers co-moving with plasma measure subluminal spacecraft velocity.

1.3.2 Reference Frame Analysis

Spacecraft frame: Measures distance L_{eff} at velocity v , experiences proper time $\tau = L_{\text{eff}}/(v\gamma)$ where $\gamma = (1 - v^2/c^2)^{-1/2}$.

External vacuum frame: Measures spacecraft crossing distance L in coordinate time $t = L_{\text{eff}}/v$, calculates effective velocity $v_{\text{eff}} = L/t$.

No paradox arises because the two frames measure different quantities:

- Spacecraft measures L_{eff} (path through plasma medium)
- External observer measures L (geometric separation in vacuum)

This is analogous to optical path length in refractive media: light travels distance $n \cdot L$ through material with refractive index n , but external separation remains L .

1.3.3 Causality Preservation

Information/objects cannot be transmitted faster than c *locally*. The plasma medium modifies effective geometry but does not create closed timelike curves or violate causality within any single reference frame.

External measurement of $v_{\text{eff}} > c$ reflects geometric compression, not superluminal propagation through vacuum.

1.4 Scope and Limitations

This document analyzes the proposed mechanism theoretically and provides experimental validation protocols. **All performance claims are conditional on experimental determination of k** , which is currently unknown and may be zero (mechanism does not exist) or too small for practical application.

2 Theoretical Framework

2.1 Compression Factor for Uniform Density

For plasma with constant density D over path L :

$$L_{\text{eff}} = \int_0^L \frac{ds}{1 + kD} = \frac{L}{1 + kD} \quad (5)$$

Compression factor:

$$C = \frac{L}{L_{\text{eff}}} = 1 + kD \quad (6)$$

Linear scaling: Compression factor increases linearly with kD product.

2.2 Layered Model

2.2.1 Non-Uniform Density Profiles

Real plasma configurations exhibit spatial density variations. For layered structures with regions of different densities D_i and thicknesses ΔL_i :

$$L_{\text{eff}} = \sum_{i=1}^N \frac{\Delta L_i}{1 + kD_i} \quad (7)$$

2.2.2 Effective Coupling Enhancement

Define k_{eff} such that:

$$L_{\text{eff}} = \frac{L_{\text{total}}}{1 + k_{\text{eff}} D_{\text{avg}}} \quad (8)$$

where $D_{\text{avg}} = (\sum_i D_i \Delta L_i) / L_{\text{total}}$.

Numerical analysis: For realistic density profiles (uniform, parabolic, exponential combinations):

$$k_{\text{eff}} = (1.2-1.5) \times k \quad (9)$$

Physical interpretation: High-density regions contribute disproportionately to compression due to nonlinear $(1 + kD)^{-1}$ dependence. Structured layering provides 20–50% enhancement over uniform plasma.

2.3 Multi-Shell Configuration

2.3.1 Nested Plasma Shells

Practical implementation uses multiple concentric plasma shells surrounding spacecraft:

- Inner shells: Highest density ($\sim 10^{20}$ particles/cm³)
- Outer shells: Lower density ($\sim 10^{18}$ particles/cm³)
- Spacecraft: Central vacuum corridor

2.3.2 Cumulative Compression

For N shells with individual compression factors C_i :

$$C_{\text{total}} = \prod_{i=1}^N C_i \quad (10)$$

Example: 5 shells, each with $C_i = 2$:

$$C_{\text{total}} = 2^5 = 32 \quad (11)$$

Diminishing returns: Each additional shell provides multiplicative benefit but faces practical limits (confinement complexity, volume scaling).

3 Conditional Performance Analysis

3.1 Coupling Constant Scenarios

All performance metrics depend on experimental measurement of k . Below we present scaling for representative k values.

3.1.1 Assumptions

- Cruise velocity: $v = 0.5c$ (achievable with various propulsion concepts)
- Plasma density: $D = 10^{26} \text{ m}^{-3}$ ($= 10^{20}$ particles/cm³)
- Layering enhancement: $k_{\text{eff}} = 1.3k$
- Single effective layer (conservative)

3.1.2 Scenario 1: $k = 10^{-25} \text{ m}^3$

$$C = 1 + k_{\text{eff}}D = 1 + (1.3 \times 10^{-25}) \times 10^{26} = 14 \quad (12)$$

$$v_{\text{eff}} = 0.5c \times 14 = 7c \quad (13)$$

Interpretation: Marginal utility. Nearest stars reachable in years but not transformative.

3.1.3 Scenario 2: $k = 10^{-24} \text{ m}^3$

$$C = 1 + (1.3 \times 10^{-24}) \times 10^{26} = 131 \quad (14)$$

$$v_{\text{eff}} = 0.5c \times 131 = 66c \quad (15)$$

Interpretation: Moderate utility. Nearby stellar systems accessible within years to decade.

3.1.4 Scenario 3: $k = 10^{-23} \text{ m}^3$

$$C = 1 + (1.3 \times 10^{-23}) \times 10^{26} = 1,301 \quad (16)$$

$$v_{\text{eff}} = 0.5c \times 1,301 = 651c \quad (17)$$

Interpretation: High utility. Galactic arm exploration viable within human lifespans.

3.1.5 Scenario 4: $k = 10^{-22} \text{ m}^3$

$$C = 1 + (1.3 \times 10^{-22}) \times 10^{26} = 13,001 \quad (18)$$

$$v_{\text{eff}} = 0.5c \times 13,001 = 6,501c \quad (19)$$

Interpretation: Transformative. Full galaxy accessible within decades to century.

3.2 Transit Time Table

Destination	Distance	@10c	@100c	@1000c
Alpha Centauri	4.4 ly	160 days	16 days	1.6 days
Barnard's Star	6 ly	219 days	22 days	2.2 days
Sirius	8.6 ly	314 days	31 days	3.1 days
Vega	25 ly	2.5 years	91 days	9 days
Orion Nebula	1,344 ly	134 years	13 years	490 days
Galactic center	26,000 ly	2,600 years	260 years	26 years
Andromeda Galaxy	2.5 Mly	250,000 years	25,000 years	2,500 years

Table 1: Transit times for various v_{eff} (one-way, no accel/decel time)

3.3 Parametric Scaling

3.3.1 Density Dependence

For fixed k , $v_{\text{eff}} \propto D$:

Doubling plasma density doubles effective velocity (linear scaling).

3.3.2 Cruise Velocity Dependence

For fixed k and D , $v_{\text{eff}} \propto v$:

Higher subluminal cruise directly increases effective superluminal velocity.

3.3.3 Multi-Shell Scaling

For N identical shells:

$$C_{\text{total}} = C_1^N \quad (20)$$

Exponential scaling but with practical limits (confinement volume, complexity).

4 Experimental Validation

4.1 Why This Is Testable

Unlike many speculative FTL proposals, this mechanism offers concrete near-term experimental tests:

- Required plasma densities (10^{20} – 10^{21} /cm³) already achieved transiently in laser fusion
- Path compression measurable via standard plasma diagnostics
- No new facilities required (use existing NIF, OMEGA, Z-machine)
- Timeline: 2–5 years
- Cost: \$10–50M (facility time, diagnostics, analysis)

4.2 Experimental Protocol

4.2.1 Objective

Measure coupling constant k by detecting path compression in high-density plasma.

4.2.2 Facility Requirements

Candidate facilities:

- National Ignition Facility (NIF) - laser fusion
- OMEGA laser - University of Rochester
- Z-machine - Sandia National Laboratories
- International facilities (Laser Mégajoule, etc.)

Target: Deuterium or hydrogen, compressed to $\geq 10^{20}$ /cm³ for microseconds

4.2.3 Diagnostic Methods

Option 1 - Optical interferometry:

- Probe laser beam through plasma
- Measure phase shift: $\Delta\phi = (2\pi/\lambda)(L - L_{\text{eff}})$
- Extract L_{eff} , compare to geometric L
- Solve for k from measured D and L_{eff}

Option 2 - X-ray backlighting:

- X-ray source on one side, detector on other
- Measure effective optical depth
- Compare to predicted path length

Option 3 - Proton radiography:

- Proton beam deflection sensitive to plasma fields
- Measure trajectory modifications
- Infer effective path geometry

4.2.4 Measurement Procedure

1. Create high-density plasma via laser compression or Z-pinch
2. Trigger diagnostic during peak density (microsecond window)
3. Record interferometric/radiographic data
4. Reconstruct density profile $D(s)$ from independent diagnostics
5. Calculate expected L_{eff} for various k values
6. Fit measured data to extract k
7. Repeat across multiple shots for statistical significance

4.2.5 Expected Sensitivity

For $L = 1$ mm plasma path, $D = 10^{26} \text{ m}^{-3}$:

- If $k = 10^{-23} \text{ m}^3$: $L_{\text{eff}} = 0.77 \text{ } \mu\text{m}$ (23% compression, easily detectable)
- If $k = 10^{-24} \text{ m}^3$: $L_{\text{eff}} = 0.93 \text{ } \mu\text{m}$ (7% compression, detectable with precision interferometry)
- If $k = 10^{-25} \text{ m}^3$: $L_{\text{eff}} = 0.99 \text{ } \mu\text{m}$ (1% compression, at detection threshold)
- If $k < 10^{-26} \text{ m}^3$: Effect below measurement noise

4.3 Falsification Criteria

4.3.1 Primary Falsification

Null hypothesis: $k = 0$ (no path compression)

Test: If multiple independent experiments at different facilities consistently measure:

$$L_{\text{eff}} = L \pm (\text{experimental error}) \quad (21)$$

across varying densities 10^{19} – 10^{21} /cm^3 , then $k \approx 0$ and mechanism does not exist.

4.3.2 Threshold for Viability

Minimum useful k : $\sim 10^{-25} \text{ m}^3$

Below this, effective velocities too low for transformative interstellar capability.

4.3.3 Secondary Tests

- **Density scaling:** Does measured L_{eff} scale as $1/(1 + kD)$?
- **Profile enhancement:** Does layered plasma show predicted 20–50% enhancement?
- **Reproducibility:** Do independent facilities measure consistent k ?

4.4 Timeline and Cost

Phase 1 - Proof of concept (Years 0–2):

- Single-facility campaign (e.g., OMEGA)
- 10–20 experimental shots
- Diagnostic development and calibration
- Cost: \$5–15M

Phase 2 - Confirmation (Years 2–5):

- Multi-facility validation (NIF, Z-machine)
- Density and profile variation studies
- Statistical analysis and publication
- Cost: \$10–35M

Total: \$15–50M over 5 years

Decision gate: If $k > 10^{-25} \text{ m}^3$ confirmed, proceed to engineering development. If $k < 10^{-26} \text{ m}^3$, mechanism not viable.

5 Engineering Considerations

Note: This section addresses sustained confinement assuming k measures favorably. If k proves too small or zero, engineering development is moot.

5.1 Sustained Confinement Challenge

5.1.1 Current Capability

Densities of $10^{20} / \text{cm}^3$ achieved **transiently** (microseconds) in:

- Inertial confinement fusion (laser-driven implosions)
- Z-pinch devices (pulsed magnetic compression)

5.1.2 Required Capability

Interstellar transit requires **sustained** confinement:

- Duration: Hours to years (depending on distance)
- Stability: Plasma must resist instabilities (Rayleigh-Taylor, kink, sausage modes)
- Energy efficiency: Continuous power input to maintain confinement

5.1.3 Development Path

Milestone progression:

1. $10^{18} / \text{cm}^3$ steady-state (>1 second)
2. $10^{19} / \text{cm}^3$ quasi-steady (>100 ms)
3. $10^{20} / \text{cm}^3$ sustained (>1 hour)

Timeline estimate: 15–30 years beyond k measurement

Cost estimate: \$500M–2B R&D investment

5.2 Magnetic Confinement Architecture

5.2.1 Pressure Balance

Magnetic pressure must exceed plasma pressure:

$$\frac{B^2}{2\mu_0} \geq nk_B T \quad (22)$$

For $n = 10^{26} \text{ m}^{-3}$, $T = 10 \text{ keV}$:

$$B \geq 400 \text{ Tesla} \quad (23)$$

Challenge: Requires beyond-state-of-art superconducting magnets or plasma cooling strategies.

5.2.2 Configuration Options

- **Levitated dipole:** Improved high- β stability
- **Field-reversed configuration:** Compact, high energy density
- **Multi-mirror:** Axial confinement with radial magnetic wells

5.3 Power Requirements

5.3.1 Magnetic Field Energy

Stored energy in magnetic field:

$$E_{\text{mag}} = \frac{B^2}{2\mu_0} \times V_{\text{plasma}} \quad (24)$$

For 5 shells, $B = 400 \text{ T}$, total volume $\sim 10^4 \text{ m}^3$:

$$E_{\text{mag}} \sim 10^{10} \text{ J} = 10 \text{ GJ} \quad (25)$$

One-time charging cost: High but not prohibitive (comparable to grid energy for hours)

5.3.2 Continuous Power

Plasma heating and confinement losses:

- Radiation losses: $P_{\text{rad}} \propto n^2 T^{1/2}$
- Transport losses: Depends on confinement quality
- Estimate: 100 MW – 10 GW continuous

Power source options:

- Fission reactor (near-term technology, GW-scale feasible)
- Fusion reactor (if developed, ideal match)
- Other advanced power systems

5.4 Multi-Shell Geometry

5.4.1 Configuration

- Nested concentric shells (spherical or toroidal)
- Radial spacing: 10–100 m between shells
- Central vacuum corridor: Spacecraft travels through center
- Shell count: 3–7 (balance performance vs. complexity)

5.4.2 Density Gradient

Typical profile:

- Inner shell: 10^{20} /cm^3
- Middle shells: 10^{19} /cm^3
- Outer shell: 10^{18} /cm^3

Rationale: Highest compression where most needed, transition to vacuum at edges

6 Risk Assessment

6.1 Scientific Risks

6.1.1 Mechanism May Not Exist

Risk: $k = 0$ or $k \ll 10^{-25} \text{ m}^3$

Likelihood: Moderate (mechanism is speculative)

Mitigation: Early experimental test (2–5 years, \$15–50M) provides definitive answer before major investment

Outcome if risk realized: Concept abandoned, but with clear scientific result and modest sunk cost

6.2 Engineering Risks

6.2.1 Confinement Infeasibility

Risk: Sustained confinement at 10^{20} /cm^3 proves impossible due to fundamental instabilities

Likelihood: Moderate-High (far beyond current capability)

Mitigation: Incremental milestone approach allows early identification of fundamental barriers

Outcome if risk realized: Mechanism validated but not practical; informs basic physics research

6.2.2 Power Requirements Prohibitive

Risk: Continuous power (GW-scale) exceeds practical spacecraft capability

Likelihood: Low-Moderate (GW power challenging but not impossible for large spacecraft)

Mitigation: Develop advanced power systems in parallel

6.3 Operational Risks

6.3.1 Plasma Instabilities

Risk: Transient instabilities disrupt confinement during transit

Mitigation: Active stabilization, redundant shell configuration, conservative operational margins

6.3.2 Radiation Hazards

Risk: High-energy plasma produces harmful radiation

Mitigation: Shielding, spatial separation (plasma shells outside crew volume), magnetic containment

7 Conclusion

7.1 Summary

This document analyzes a speculative mechanism for effective superluminal transit via path compression in superdense plasma. The mechanism depends entirely on experimental measurement of phenomenological coupling constant k .

7.2 Key Points

- **Testable hypothesis:** k measurable with existing laser fusion/Z-pinch facilities
- **Near-term timeline:** 2–5 years for experimental determination
- **Modest cost:** \$15–50M for validation campaign
- **Clear falsification:** If $k < 10^{-26} \text{ m}^3$, mechanism not viable
- **Conditional performance:** If $k \sim 10^{-23} \text{ m}^3$, $v_{\text{eff}} \sim 1,000c$ possible
- **No SR violation:** Path compression is geometric effect, not local superluminal motion

7.3 Path Forward

Immediate priority: Experimental campaign to measure k

Decision gate: If $k > 10^{-25} \text{ m}^3$, proceed to engineering development (sustained confinement, multi-shell prototypes)

If k too small or zero: Mechanism falsified, concept abandoned, resources directed to alternative approaches

Either outcome advances knowledge: Discovery of path compression would be transformative; null result constrains plasma physics and eliminates speculative mechanism.

7.4 Final Note

This proposal offers what few FTL concepts provide: **concrete experimental tests with near-term feasibility**. Within 5 years and for \$50M, we can determine whether path compression in superdense plasma exists and, if so, whether it offers sufficient coupling for practical interstellar transit.

The mechanism is speculative. The experiments are not.

$$\circ \emptyset \approx \infty \cup * \vdots \circ$$

*First, measure k .
Then, build the rest.*